

# WASTEWATER OPERATOR MATH CHEAT SHEET

Formulas, conversions, and the "why" behind them — built by a licensed operator

## CRITICAL CONVERSIONS

The conversions behind almost every loading, dosage, and flow problem on the exam. Memorize them cold.

1 ft <sup>3</sup>	= 7.48 gallons	1 cfs	= 448.8 gpm
1 gallon (water)	= 8.34 lbs	1 cfs	= 0.6463 MGD
1 mg/L	= 1 ppm	1 MGD	= 694.4 gpm
1% concentration	= 10,000 mg/L	1 MGD	= 1.547 cfs
1 lb	= 453.6 grams	1 gpm	= 1,440 gpd
1 acre-foot	= 325,851 gallons	1 hp	= 33,000 ft-lb/min
1 ft (water column)	= 0.433 psi	1 hp	= 0.746 kW
1 cubic yard	= 27 ft <sup>3</sup>	π (pi)	= ≈ 3.14

## THE 8.34 RULE (most important number on the exam)

### 1 gallon of water weighs 8.34 lbs

This is the heart of the pounds-per-day formula — BOD loading, solids loading, and chemical dosing all run through it. If you forget every other conversion, remember this one.

## GEOMETRY & VOLUME

### Rectangle area = L × W    Circle area = $0.785 \times D^2$ (or $\pi \times r^2$ )

0.785 equals  $\pi/4$ , so you can use the diameter directly instead of converting to a radius.

### Cylindrical tank volume = $0.785 \times D^2 \times \text{height}$

Round tanks, clarifiers, digesters, contact basins. Answer is in ft<sup>3</sup> when D and h are in feet.

### Rectangular tank volume = L × W × H

All dimensions in feet → answer in ft<sup>3</sup>. Multiply by 7.48 to get gallons.

## FLOW, VELOCITY & DETENTION TIME

### Flow (Q) = Velocity × Area    Velocity = Flow ÷ Area

### Detention time = Volume ÷ Flow rate

Keep units consistent. If volume is in gallons, flow must be in the same time unit you want the answer in (gpm → minutes, gpd → days). For hours from gpd: × 24.

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## LOADING — THE POUNDS FORMULA

$$\text{Pounds per day} = \text{Concentration (mg/L)} \times \text{Flow (MGD)} \times 8.34$$

The workhorse of wastewater math. Use it for BOD load, TSS/solids load, and chemical feed. Units must be mg/L and MGD — if flow is in gpm, divide by 694.4 first.

$$\text{BOD loading (lb/day)} = \text{BOD (mg/L)} \times \text{Flow (MGD)} \times 8.34$$

The organic load applied to the plant or the aeration basin — the numerator of the F/M ratio below.

## ACTIVATED SLUDGE PROCESS CONTROL

$$\text{F/M ratio} = \text{lb BOD applied per day} \div \text{lb MLVSS under aeration}$$

Food-to-microorganism ratio. Conventional activated sludge typically runs ~0.2–0.5. Uses MLVSS, not MLSS.

$$\text{MCRT / SRT (days)} = \text{lb MLSS in the system} \div \text{lb solids leaving per day}$$

Mean cell residence time. Solids leaving = WAS solids + effluent solids per day. The master control variable.

$$\text{Sludge age (days)} = \text{lb MLSS under aeration} \div \text{lb TSS entering per day}$$

Gould sludge age — a simpler approximation than MCRT that ignores solids in the clarifier.

$$\text{SVI (mL/g)} = (\text{30-min settled volume in mL/L} \times 1,000) \div \text{MLSS (mg/L)}$$

Sludge Volume Index. Good settling is roughly 80–120. High SVI signals bulking; very low can mean pin floc.

$$\text{Return sludge rate (\%)} \approx \text{SSV}_{30} \div (1,000 - \text{SSV}_{30}) \times 100$$

Settleometer estimate of RAS rate as a percent of influent flow, where  $\text{SSV}_{30}$  is the 30-minute settled volume (mL/L).

## SECONDARY CLARIFIER

$$\text{Surface overflow rate (gpd/ft}^2\text{)} = \text{Flow (gpd)} \div \text{Surface area (ft}^2\text{)}$$

Secondary clarifiers typically run ~400–800 gpd/ft<sup>2</sup>. Too high carries solids over the weir.

$$\text{Solids loading rate (lb/day/ft}^2\text{)} = \text{Solids applied (lb/day)} \div \text{Surface area (ft}^2\text{)}$$

Includes MLSS carried in on the influent + RAS. Secondary clarifiers usually run ~20–30 lb/day/ft<sup>2</sup>.

$$\text{Weir overflow rate (gpd/ft)} = \text{Flow (gpd)} \div \text{Weir length (ft)}$$

High weir loading drags floc over the launders.

## DISINFECTION

$$\text{Chlorine dose} = \text{Chlorine demand} + \text{Chlorine residual} \quad \text{CT} = \text{C (mg/L)} \times \text{T (min)}$$

Dose is what you feed; residual is what's left after demand is satisfied. CT must meet your permit's target.

## SOLIDS & DIGESTION

$$\text{Dry solids (lb/day)} = \text{Sludge flow (MGD)} \times 8.34 \times \% \text{ solids (as a decimal} \times 100)$$

Quick form: lb/day = gallons × 8.34 × (% solids ÷ 100). 1% solids means 10,000 mg/L.

$$\text{Volatile solids loading (lb VS/day/ft}^3\text{)} = \text{lb VS added per day} \div \text{digester volume (ft}^3\text{)}$$

Standard-rate digesters run low (~0.04–0.1); high-rate digesters run higher (~0.1–0.3).

## PERCENT REMOVAL (EFFICIENCY)

$$\text{Percent removal} = ((\text{In} - \text{Out}) \div \text{In}) \times 100$$

Used for BOD and TSS removal efficiency. In and Out must be the same units (usually mg/L).

## WASTEWATER MATH TIPS

- ✓ Underline what you're solving for (lb/day? gpd/ft<sup>2</sup>? days?). Wrong unit = wrong answer.
- ✓ Convert flow to MGD before using the 8.34 formula. Always. If you have gpm, divide by 694.4.
- ✓ MLVSS for F/M; MLSS for SVI and MCRT — don't mix the two up.
- ✓ Estimate first, then round only at the very end. Mid-problem rounding compounds fast.